

A New Bias Field Correction Method Combining N3 and FCM for Improved Segmentation of Breast Density on MRI

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ABSTRACT:

25 **Purpose:** Quantitative breast density is known as a strong risk factor associated with development of breast cancer. Measurement of breast density based on 3-dimensional breast MRI may provide very useful information. One important step for quantitative analysis of breast density on MRI is the correction of field inhomogeneity to allow an accurate segmentation of fibroglandular tissue (dense tissue). A new bias-field correction method by combining the N3 (nonparametric
30 nonuniformity normalization) algorithm and Fuzzy-C-Means (FCM)-based inhomogeneity correction algorithm is developed in this work.

Methods: The analysis is performed on non-fat-sat T1-weighted images acquired using a 1.5T MRI scanner. This algorithm utilizes the advantages of both N3 and FCM algorithms. N3 is known as a robust correction method, but it cannot correct a strong bias-field on a large area.
35 FCM-based algorithm can correct the bias-field on a large area, but it may change the tissue contrast and affect the segmentation quality. The proposed algorithm applies N3 first, followed by FCM, and then the generated bias-field is smoothed using Gaussian kernel and B-spline surface fitting to minimize the problem of mistakenly changed tissue contrast. The process is repeated until the number of corrected pixels is fewer than 5% of the total number of pixels in the
40 whole breast. The segmentation results based on the N3+FCM corrected images and the N3 and FCM alone corrected images were presented to a radiologist in a random fashion for evaluation. The performances of three methods in a total of 60 breasts from 30 healthy volunteers were ranked.

Results: We demonstrated that the iterative N3+FCM method can gradually correct a strong

45 bias-field presented on the original images without mistakenly changing the tissue contrast. The correction brightens the signal intensity of fatty tissues, and that separates the histogram peaks between the fibroglandular and fatty tissues to allow an accurate segmentation between them. In the first reading session, the radiologist found ($N3+FCM > N3 > FCM$) ranking in 24 breasts; ($N3+FCM = N3 > FCM$) in 32 breasts; ($N3+FCM = N3 = FCM$) in 2 breasts; and ($N3 >$
50 $N3+FCM > FCM$) in 2 breasts. The results of the second reading session were similar, even more in favor of the N3+FCM method. The performance in each pair-wise Wilcoxon signed-rank test is significant, showing N3+FCM superior to both N3 and FCM, and N3 superior to FCM.

Conclusions: Choosing an appropriate bias-field correction method is a very important preprocessing step to allow an accurate segmentation of fibroglandular tissues based on breast
55 MRI for quantitative measurement of breast density. The proposed algorithm combining N3+FCM yields satisfactory results.

Key Words: bias field, field inhomogeneity correction, fibroglandular tissue segmentation

I. INTRODUCTION

60 Breast density has been proven as an independent risk factor associated with the
development of breast cancer.¹⁻⁴ With the strong evidence, the Breast Cancer Prevention
Collaborative Group (BCPCG) recommended that breast density should be incorporated into the
risk prediction model to improve the accuracy of predicting each individual woman's cancer
risk.⁵ However, all supporting evidence to date was established based on the density analyzed on
65 mammography. Since the density measurement is based on a 2-D projection image, it may vary
with different body positions, level and angle of compressions, and the setting of X-ray source
and detector. The variations in the measured mammographic density may lead to different
estimates of cancer risk.

Breast MRI acquires 3-D images, and provides a strong contrast between fibroglandular
70 tissue (i.e. dense tissue) and fatty tissue for measurement of density. The MRI-based analysis
methods have been published by several groups⁶⁻¹³, and the results from large series comparing
MRI density with mammographic density have started to come out in the literature.¹⁴⁻¹⁶ We have
published a complete processing method for quantitative measurement of breast density, which
includes breast segmentation, intensity inhomogeneity (bias field) correction and tissue
75 classification using the fuzzy C-means (FCM) algorithm.⁶ Although this method has been
successfully applied to analyze the density on non-fat-sat T1-weighted images that were acquired
using a 1.5 T MRI scanner,⁶⁻⁹ the segmentation performance based on images that were acquired
using a newer scanner with a flat-bed breast coil is not satisfactory. Due to the strong intensity
inhomogeneity near the posterior breast, the fatty tissues near the pectoral muscle have low
80 signal intensities and often are mis-classified as dense tissues. That is, the FCM algorithm is not

sufficient to perform the bias-field correction, and other inhomogeneity correction method is needed.¹⁷

Intensity inhomogeneity (or, bias field herein) often presents as a smooth intensity variation across the image and is mainly coming from poor radio frequency (RF) coil uniformity, gradient-driven eddy currents, and patient anatomy both inside and outside the field of view (FOV).¹⁷ In general, inhomogeneity correction can be done prospectively based on adjustments of hardware and acquisition methods, or retrospectively based on post-scan image processing. Prospective correction methods include using phantom-based calibration of bias field,¹⁸ multicoil scan¹⁹ and special imaging sequences.²⁰ However, prospective methods can only remove the inhomogeneity associated with the scanner, not the scanned subject, and retrospective correction methods are needed to remove the subject dependant inhomogeneity.

Four retrospective correction methods are commonly used.¹⁷ The first method uses filtering, which assumes bias field as a low-frequency artifact,²¹⁻²² but this assumption is only applicable for relatively small structures. The second method is based on surface fitting of intensity²³ or gradient²⁴ field, and it mainly works for images that have relatively large and distinctive homogeneous areas. The third method is based on the iterative process of bias field estimation, which requires *priori* knowledge of different structures for segmentation, e.g. gray matter and white matter in the brain.²⁵⁻²⁶ The forth method is based on histogram, which does not require *priori* knowledge and can be applied to large areas with different anatomical structures.²⁷⁻²⁸

In our previous breast density segmentation method based on MRI, the FCM algorithm was used for both homogeneity correction and segmentation.²⁹ This algorithm enhances the signal intensity of fatty tissues within the low sensitivity region of the coil, but the intensity of some

fibroglandular tissues is also further enhanced, and that may change the overall contrast of images leading to wrong segmentation results. The N3 (nonparametric nonuniformity normalization) algorithm²⁷ is a fully automatic histogram-based method, and is a popular correction method widely used in the literature. The N3 algorithm is able to reduce the bias field while avoiding the problem of generating erroneous contrast. However, the N3 algorithm was originally developed for brain images which has a smaller field of view and generally presents much less inhomogeneity than the breast images, and it may not be sufficient for bias-field correction of breast images.

The purpose of this work is to develop an iterative correction scheme utilizing the combination of N3 and FCM-based algorithms (noted as N3+FCM). The field inhomogeneity was first removed by using the N3 followed by the FCM-based algorithm and B-spline surface fitting,²⁷ and then the process was repeated iteratively until the correction is completed. The corrected images were then segmented to differentiate between fibroglandular and fatty tissues. The quality of the segmentation results obtained using the proposed N3+FCM correction method and that obtained using the FCM-based correction alone and the N3 algorithm alone were compared.

120 **II. MATERIALS AND METHODS**

II.A. Subjects

This study recruited 30 healthy subjects (age 23-61, mean 35), including 25 pre-menopausal (mean 30 years old) and 5 post-menopausal women (mean 58 years old). Since both breasts in each subject were analyzed separately, a total of 60 breasts were studied. All subjects did not

125 have any symptom of breast discomfort or palpable breast mass. None of the subjects received
hormonal replacement therapy, took oral contraceptives, or had prior history of breast disease or
treatment. This study was approved by the institutional review board and all participants gave
written informed consent.

Breast MRI was performed using a 1.5T scanner (Siemens, Erlangen, Germany). One set of
130 3D T1-weighted images without fat saturation was acquired using the FLASH sequence. The
imaging parameters were TR/TE = 11/4.7 msec; flip angle = 20 degrees; FOV = 35 cm; slice
thickness = 2mm; and matrix = 256x256. The total imaging time for this sequence is 2.5 min.

II.B. Breast segmentation and inhomogeneity correction

135 The first analysis step is to segment the breast region from the body. An initial cut was
performed by manually drawing a horizontal line through the posterior boundary of the sternum,
and all tissues below this line were removed. Then the procedures described in a previous
publication,⁶ including using the semi-automatic FCM-based method to extract the breast region
and using the B-spline fitting to exclude the chest wall muscle, were applied to segment out the
140 breast. For exclusion of skin and nipples, we have developed an improved method, which will be
done after the inhomogeneity correction.

We adopted a widely used concept to model the image with intensity inhomogeneity as a
smooth multiplicative field.^{17,27} The image formation can be written as:

$$V(x) = U(x)b(x) + n(x) \quad (1)$$

145 where V is the measured intensity at location x , U is the true intensity emitted by the tissue, b is
an unknown smoothly varying bias field, and n is white Gaussian noise assumed to be

independent of U . To avoid the difficulty of additive and multiplicative interference, we simplify the image model as a noise-free case, while transforming it into log space to make the bias field additive. Using the notation $\hat{I}(x) = \log[I(x)]$, the image model is rewritten as:

$$\hat{V}(x) = \hat{U}(x) + \hat{b}(x) \quad (2)$$

The purpose of the inhomogeneity correction is to estimate the bias field \mathbf{b} . The flowchart of the proposed correction method is shown in Figure 1. The first step is to apply the N3 algorithm to the original image \mathbf{I} to correct the inhomogeneity. However, it can be seen that after the N3 correction, the fatty tissues close to chest wall still appear dark. Then the FCM algorithm is applied to the N3 corrected image \mathbf{N} to further reduce the inhomogeneity, noted as \mathbf{F} . Using the simplified model in (2), the additional bias field \mathbf{B} after the FCM correction \mathbf{F} compared to after the N3 correction \mathbf{N} is calculated by:

$$\mathbf{B}(x) = \exp(\hat{N}(x) - \lambda \hat{F}(x)) \quad (3)$$

where λ is an adjustable constant factor that is used to increase the contrast of the bias field, and was defined empirically. For the 1.5T breast MR images analyzed in this study, we found $\lambda = 0.8$ generated the best result. Initially when λ was not introduced (or, set as one), the correction effect could not be visually appreciated. After this parameter was added, the value from 0.5 to 0.9 was tested in selected cases, and it was found that $\lambda = 0.8$ gave the best results for most cases. For the cases when segmentation errors were noted using $\lambda = 0.8$, the value was changed to see whether the segmentation quality could be improved. However, rarely setting λ at a different value could improve the segmentation quality. This parameter may need to be adjusted based on the quality of the original images in future studies.

The intensity ranges of both \mathbf{N} and \mathbf{F} after the N3 and FCM correction are normalized to the

range of the original image I slice by slice for further processing. In order to ensure that the bias
 170 field varies smoothly, smoothing is necessary. Figure 2 shows the process of generating the
 estimated bias field and how this bias field is used to obtain a new corrected image. The obtained
 bias field B (Fig.2c) from Eq. (3) was first smoothed by a 3×3 Gaussian kernel (Fig.2d) and then
 further smoothed by B-spline parametric surface fitting (Fig.2e). The smoothed bias field was
 then applied back to N to calculate the inhomogeneity corrected image NF using:

$$175 \quad NF_n(x) = \exp\left(N\hat{F}_{n-1}(x) - B(x)\right), \quad 1 \leq n \leq \max_iter \quad (4)$$

$$\text{with } N\hat{F}_0(x) = \hat{N}(x).$$

After correcting the bias-field using B to obtain the image NF (Fig.2f), an additional step
 was applied to make sure that the intensity of any pixel within the image field is brighter than
 their intensity in the previous iteration, as:

$$180 \quad C_n(x) = \max(NF_n(x), C_{n-1}(x)), \quad 1 \leq n \leq \max_iter \quad (5)$$

$$\text{with } C_0(x) = \max(I(x), N(x))$$

This step is necessary because some fatty tissue pixels close to the fibroglandular tissue may be
 smoothed out and has a lowered signal intensity after the bias field correction. For these fatty
 tissue pixels, the lowered intensity will decrease their contrast from the nearby dense tissue pixels,
 185 and lead to segmentation error. Therefore, for these pixels, their brighter intensities in the
 previous iteration will be kept. As will be shown later, one main purpose of the bias field
 correction is to increase the dynamic range, particularly to brighten the signal of the fatty tissues
 so they can be separated from the fibroglandular tissues, so this step is needed to ensure that the
 intensity of fatty tissues will increase after each iteration.

190 This process combining N3 and FCM will be repeated until the bias field does not change

any more. Since the main purpose of the bias-field correction is to brighten the intensity of fatty tissue pixels, the stopping criteria are defined based on the number of pixels that show an intensity change $> i_{thd}$. When fewer than 5% of the total number of pixels in the whole breast shows changes, the iteration will stop. Define SC_n as the absolute value of the difference between C_n and C_{n-1} , then the number of pixels with intensity change greater than i_{thd} can be counted by the pixels that show $SC_n(x) > i_{thd}$. In this study, the threshold was set as $i_{thd} = \max(SC_0)/256$. Using this threshold, the correction in most cases was completed between 10-20 iterations. The iteration process stops when one of the following conditions is met: 1) the number of pixels showing intensity change greater than i_{thd} is less than 5% of the total number of pixels in the whole breast area; 2) the number of iteration exceeds the maximum, which was set as 20 in this work. The example shown in Figure 1 takes 10 iterations to reach the stopping criteria, and the corrected images after the first, sixth, and tenth iterations are shown in Figure 1. Figure 3 shows the subtraction image SC_n after each iteration. It clearly demonstrates that during the iteration process the areas showing changes (coded by color) are shrinking from the nipple to the chest wall, indicating that more severe inhomogeneity occurs in the region close to the chest wall, and more iterations are needed to correct pixels in that region.

II.C. Fibroglandular tissue segmentation

The skin and nipple show similar intensities compared to that of fibroglandular tissue, and need to be removed. In our previous study,^{6,8} skin was identified using dynamic search based on the gradient of the signal intensities perpendicular to the skin layer. However, nipple often connects to the fibroglandular tissue and cannot be defined based on gradient search, and a fixed

layer of 3 pixels (approximately 5 mm) was excluded. Generally, breast boundary follows a smoothly varying curve and nipple at a prone position is protruding from the breast curve. After setting up the control points of breast boundary, the breast boundary was fit into a smooth curve using Bezier splines:³⁰

$$\left\{ \begin{array}{l} x(u) = \sum_{k=0}^{p-1} x_k BEZ_{k,p-1}(u) \\ y(u) = \sum_{k=0}^{p-1} y_k BEZ_{k,p-1}(u) \\ BEZ_{k,p}(u) = \frac{(p-1)! u^k (1-u)^{p-k-1}}{k!(p-k-1)!}, \quad 0 \leq u \leq 1 \end{array} \right. \quad (6)$$

where p is the number of control points. The fitted breast boundary removed the major area of nipple, and then within the remaining breast area the dynamic search algorithm was applied to find and extract the skin. On the non-fat-sat T1 weighted images, the background signal is dark, the skin signal is intermediate, and the fatty tissue signal is bright, and the skin is defined as the layer in between the two gradients.

In the skin and nipple excluded breast region, the FCM clustering algorithm was applied to segment the fibroglandular tissue. Typically a total of 6 FCM clusters were used, brighter 3 as the fatty tissues and the darker 3 as the fibroglandular tissue. If the segmented dense tissues using the default setting is consistently over-estimated or under-estimated, the operator may change the setting of cluster numbers.⁶

The source C++ codes of N3 algorithm and B-spline fitting algorithm was taken from this website: packages.bic.mni.mcgill.ca/tgz. Since the iterative process of inhomogeneity correction and the segmentation process were written in MATLAB, the C++ codes were modified to be compiled in MATLAB using GNUMEX (<http://gnumex.sourceforge.net/>) and MINGW

(<http://www.mingw.org/>). The computational time of the entire segmentation process including inhomogeneity correction mainly depends on the iterations of correction. For a desktop computer (Intel Quad 2.8GHZ, 8G RAM), the typical computational time ranges from 20 to 90 seconds.

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II.D. Evaluation of segmentation quality by three methods

The segmented images using three different inhomogeneity correction methods (FCM-based, N3, and the new method using N3+FCM) were visually evaluated by an experienced radiologist, and the segmentation accuracy among these three sets was ranked. These three sets were
240 presented in a random order noted by (A, B, and C) to ensure a fair review. Using the original non-segmented images as references, the radiologist evaluated the segmentation quality slice-to-slice. The evaluation criteria include the number of slices in which a noticeable portion of breast tissues were wrongly assigned (fatty tissues as fibroglandular tissues, or vice versa), as well as the area of wrongly segmented tissues on each slice. After completing the evaluation of all
245 three sets of images for each breast, the radiologist determined the best, the second best, and the worst (e.g. $A > B > C$), or equal quality (e.g. $A = B > C$ or $A = B = C$). To assess the consistency of radiologist's evaluation, the rating was done twice with one month interval in between.

II.E. Statistical analysis

250 The pair-wise Wilcoxon signed-rank test was applied to assess whether or not the superiority exists between the segmentation accuracy based on images generated using different correction methods. The performance between each pair of N3, FCM, and N3+FCM was tested. A p-value less than 0.05 was considered significant.

255 **III. RESULTS**

III.A. Comparison of inhomogeneity correction

Since the purpose of inhomogeneity correction is to improve the accuracy of fibroglandular tissue segmentation, the comparison is made using the segmentation quality as the evaluation metrics. Figure 4 shows an example of the comparison on one image slice. The original image with heavy bias field, and the corrected images using FCM-based, N3, and the proposed N3+FCM are presented in the top row. In the middle row, the goldstandard fibroglandular tissue manually delineated by the radiologist, and the corresponding fibroglandular tissue segmentation results based on FCM, N3, and the new N3+FCM corrected images are shown. The fibroglandular tissue segmentation based on N3+FCM corrected image is the closest to the goldstandard, thus the most accurate among the three methods. Both FCM-based and N3 corrected images lead to mis-classification of posterior fatty tissues as fibroglandular tissues. For FCM-based correction, some fibroglandular tissues in the anterior region of the breast close to the nipple are brightened so much resulting in mis-classification as fatty tissues. Therefore, the FCM-based correction is the worst among all three methods. The corresponding histograms of the pixels in the truth fibroglandular tissue and fatty tissue regions (based on radiologist's manual segmentation) analyzed from the original image, FCM-based, N3 and the N3+FCM correction are shown in the bottom row. For FCM-based correction, the histograms of fibroglandular tissue and fatty tissue still have a substantial overlap, only slightly better compared to the overlap in the original histograms without correction. The peaks of FCM-corrected histograms shift to the right (towards higher intensity range), indicating that both fibroglandular and fatty tissues are

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brightened. This result clearly shows that the FCM-based correction is not sufficient to allow an accurate segmentation. The N3 algorithm widens the separation between the two histogram peaks. The proposed N3+FCM is the best, showing a clean separation of these two histogram peaks, thus allows a clean differentiation between fibroglandular tissues and fatty tissues to achieve the most accurate segmentation result among these three methods.

III.B. Comparison of segmentation quality

The visual evaluation results of the segmentation quality made by the radiologist in two separate reading sessions are summarized in Table-1. All together there are a total of 60 breasts. In the first reading session, the ($N3+FCM > N3 > FCM$) ranking is found in 24 breasts, i.e. the performance of N3+FCM is better than using N3 alone, and also the performance using N3 is better than using FCM. The ($N3+FCM = N3 > FCM$) ranking is found in 32 breasts, i.e. the performance using N3+FCM and using N3 alone is equivalent, and they are better than using the FCM. The ($N3+FCM = N3 = FCM$) ranking is found in 2 breasts, i.e. the performance using all three methods is equivalent. The ($N3 > N3+FCM > FCM$) ranking is found in 2 breasts, i.e. the performance using the N3 alone is better than using N3+FCM. The results of the second reading session are slightly different, but overall it also shows that in most cases the proposed N3+FCM is better or equal to using N3 alone, and that the FCM method is the worst. Figures 5-7 show examples of three different comparison results. For the case shown in Figure 7, all three correction methods can lead to an accurate segmentation. Compared to the other cases shown in Figures 5 and 6, the breast shown in Figure 7 is much smaller (especially in terms of the protruding depth of the breast into the coil), and the signal intensity is homogeneous on the entire

image. For this case without a strong bias-field, the correction is probably not needed, and all three methods yield satisfactory results.

300 The significance level between each pair of methods was evaluated using the Wilcoxon signed-rank test. In the first reading session, the N3+FCM is better than N3 in 24 cases, with equal performance in 34 cases, and worse than N3 in 2 cases. The Wilcoxon test shows that N3+FCM is significantly better than N3, with $p < 0.001$. The N3+FCM is better than FCM in 58 cases and with equal performance in 2 cases; also the N3 is better than FCM in 58 cases and with
305 equal performance in 2 cases; and both comparisons are significant with $p < 0.001$. The results of the second reading session were more in favor of N3+FCM. The N3+FCM is better than N3 in 28 cases, with equal performance in 31 cases, and worse than N3 in only 1 case. Therefore, overall the proposed N3+FCM method is superior compared to the FCM or the N3 method, and that the N3 is significantly better than the FCM method.

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IV. DISCUSSION

We propose a new bias field correction method using iterative N3 and FCM-based algorithm, and have demonstrated that this new correction method can be used to improve the accuracy in segmentation of fibroglandular tissue. The bias-field correction and segmentation are fully
315 automatic and require no manual operation in most cases. The most noticeable benefit of the N3+FCM correction method is in its ability to correct the strong bias-field near the posterior breast. Tissues in this area falls in the low sensitivity region of the coil, which makes the fatty tissues appear dark and mis-classified as the fibroglandular tissue. The proposed N3+FCM algorithm can be used to brighten the fatty tissue in this area without affecting the intensity of the

320 fibroglandular tissue elsewhere.

The motivation of this work came from the poor performance of the FCM-based correction method in the presence of a strong bias-field. Although the FCM method worked well in our previous datasets acquired using a close-form breast coil,⁶⁻⁹ for images acquired using the flat-bed breast coil this method could not correct the strong bias-field, and often led to wrong
325 segmentation results. Because the optimization function of FCM is designed to detect local valleys instead of global minimum, the FCM-based correction is very sensitive to noise. Therefore, in our previous approach an iterative low-pass filter was added to smooth the neighborhood in the standard objective function of FCM algorithm.⁶ However, this smoothing filter may cause problem in a large breast, where fatty tissues along the boundary of the chest
330 wall may be smoothed out to be close to the outside background. In addition, this correction method assumes that the bias field is of low spatial frequency and other components in the residual image have higher frequencies, which is usually not true for cases with dense breasts, and the correction would lead to erroneous contrast between fibroglandular tissue and fat, as shown in Figure 4.

335 Since the N3 algorithm was the most well-established inhomogeneity correction method, it was implemented to test its correction effect on breast images. N3 can detect the smooth, slowly varying, multiplicative field that maximizes the high frequency content of the distribution of the tissue intensities. Although it is originally designed for brain MRI, since the *priori* knowledge regarding segmentation is not required, this algorithm is applicable to breast MRI as well. In a
340 recent review paper about inhomogeneity correction, N3 is still considered as an optimal and widely applicable method.¹⁷ However, the test results using the N3 algorithm for inhomogeneity

correction still showed problems (in Figure 4) and could not allow an accurate segmentation.

This was probably due to the much larger size of the breast compared to the brain, as well as the design of the breast coil as a surface coil not a volume coil.

345 Inspired by the advantages and drawbacks of the two correction methods, we proposed to combine them, and further use the iterative approach to optimize the quality of the correction. How these two methods are combined to improve the correction is illustrated in Figure 2. Unlike the FCM-based correction, the optimization of the N3 algorithm does not depend on local minima,²⁷ so it will not change the overall contrast between fibroglandular tissue and fatty tissue on the image. Therefore, the N3 algorithm was applied first to make the initial correction (Fig.2a), and then the FCM-based correction is applied to further correct the inhomogeneity (Fig.2b). But as shown in Fig.2b, although the fatty tissues in the posterior breast are brightened, some fibroglandular tissues in the anterior breast are also brightened. In order to suppress this erroneous change of contrast due to local minima, B-spline surface fitting is applied to smooth the estimated bias field. This is an important process to fully utilize the advantage of FCM and minimize the impact of erroneous contrast. As shown in Figure 3, this process combining N3, FCM, and B-spline surface fitting can be repeated iteratively, and the area that needs bias field correction is shrinking after each iteration.

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The new algorithm combining N3+FCM yields a significant improvement in the segmentation quality. As shown in the radiologist's blind evaluation results, during the first reading session, the combined approach is superior to N3 in 24 of the 60 breasts, with equality quality in 34 cases, and inferior in only 2 cases. A more favorable result was found in the second reading session.

The combined approach is superior to N3 in 28 cases, with equality quality in 31 cases, and

inferior in only 1 case. Figures 5 to 7 show three examples. It can be seen that for cases with a
365 very strong bias-field (e.g. Figure 5), N3+FCM is better than N3, and both are better than FCM.
For cases without a discernable bias-field (e.g. Figure 7), correction is probably not needed, and
all three methods produce good segmentation quality and are rated equally. Therefore, the choice
of the correction method should be dependent on the quality of the image. The results based on
these 3 case examples suggest that for a large breast that protrudes deep into the flat-bed breast
370 coil, the coil cannot produce a large homogeneous field to cover the whole breast, and
consequently the acquired images show a strong field inhomogeneity. On the other hand, for a
small breast that does not protrude deep, the coil can produce a homogeneous field to cover the
whole breast, and the acquired images do not show a strong field inhomogeneity. For cases with
small breasts, the FCM-based method works just as fine as the other two. The images reported in
375 our previous publication were acquired using a closed-form breast coil,⁶⁻⁹ with the breast tissue
fitted into a confined bra-shape space. The produced images are homogeneous, and FCM-based
correction method is sufficient.

In summary, in this work we described a new bias-field correction method by combining the
N3 and FCM-based inhomogeneity correction algorithm. This algorithm utilizes the advantages
380 of both N3 and FCM, and by iteration to gradually correct a strong bias-field presented on the
original images without erroneously changing the tissue contrast. It is shown that the N3+FCM
method can lead to an improved segmentation quality compared to using either the N3 or the
FCM method alone. This method is particularly useful for correcting the MR images with a
severe regional bias-field, which is commonly presented in the MR images of large breasts
385 acquired using a flat-bed breast coil. Choosing an appropriate bias-field correction method is a

very important preprocessing step to allow an accurate segmentation of fibroglandular tissues based on breast MRI for measurement of breast density.

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Table-1. Radiologist's visual ranking of the fibroglandular tissue segmentation quality based on images corrected these three methods.

	Reading-1	Reading-2
$N3+FCM > N3 > FCM$	24	28
$N3+FCM = N3 > FCM$	32	29
$N3+FCM = N3 = FCM$	2	2
$N3 > N3+FCM > FCM$	2	1

“>” means superior quality, and “=” means equal quality

The two reading sessions are one month apart, performed independently

FIGURE LEGENDS:

Figure 1. The iterative process of the N3+FCM bias field correction algorithm. The original image is noted as I . The N3 corrected image is noted as N , which still shows inhomogeneous intensity in the posterior breast. Then the FCM is applied to N to generate the corrected image, noted as F . Although the bias field shown in N is removed in F , but the intensity of some anterior fibroglandular tissue is brightened to close to the fatty tissue. The bias field B is estimated by calculating the difference between N and F in log space (illustrated in Figure 2). Then the Gaussian kernel and the B-spline surface fitting is used to smooth the bias field, so the problem of erroneously changing contrast in the anterior breast can be minimized. By the deconvolution of new smoothed bias field B from N the bias-field corrected image is generated, noted as NF . In order to keep increasing the dynamic range in the entire intensity spectrum, the intensity of each pixel on the NF is compared to the corrected image in the previous iteration (i.e. the original image I for the first iteration), and the higher intensity is used to form the corrected image C_1 after the first iteration. This process is repeated until the stopping criteria are met. For this example, 10 iterations are needed. The corrected image after the first, sixth and tenth iteration, C_1 , C_6 and C_{10} are shown.

Figure 2. The calculation of bias field for the example shown in Fig.1 during the first iteration. (a) the N3 corrected image N . (b) the FCM corrected image F using the N3 corrected image N as the input. (c) The calculated bias field by taking exponential of $(\hat{N} - \lambda \hat{F})$ using Eq.(3), with $\lambda=0.8$. The dark area in the anterior breast indicates the erroneous change of contrast that makes fibroglandular tissues appear as fatty tissues. (d) Smoothing of (c) using a Gaussian kernel. (e)

Smoothing of (d) using B-spline surface fitting to obtain the estimated bias field \mathbf{B} . The dark area
515 in the anterior breast shown in (c) and (d) is removed after the B-spline surface fitting, and the
homogeneity correction is mainly seen in the posterior breast. (f) The corrected image NF_I
calculated by the deconvolution of \mathbf{B} from N . Note that all displayed images are in a relative
scale.

520 **Figure 3.** The subtraction image between the pair of images before and after each iteration. Ten
images from iteration # 1 to #10 are shown, using a normalized scale indicated by the color bar.
They demonstrate that the areas showing intensity difference between two iterations is shrinking.
The lateral posterior breast presents the strongest field inhomogeneity, and the correction effect is
clearly seen after each iteration. The iteration will stop when the number of pixels showing
525 changes is smaller than 5% of the total number of pixels in the whole breast.

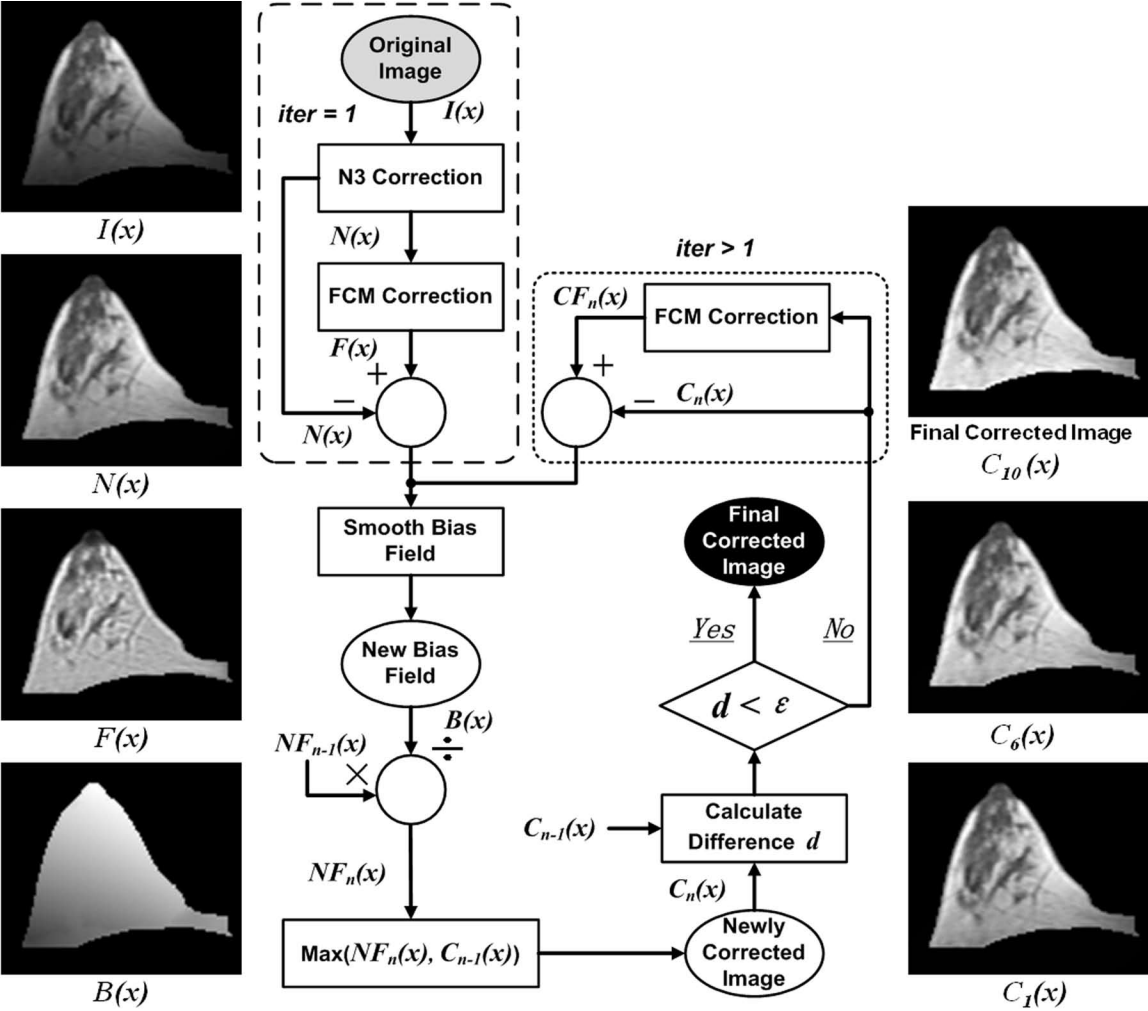
Figure 4. Comparison of the fibroglandular tissue segmentation quality based on images
corrected using three methods. The top row from left to right shows: original image, FCM
corrected image, N3 corrected image, and N3+FCM corrected image. The middle row from left
530 to right shows: the truth fibroglandular tissue delineated by a radiologist, and the segmentation
results based on FCM, N3 and N3+FCM corrected images. It can be seen that N3+FCM produces
the most accurate results close to the truth outlined by the radiologist, and FCM has the worst
segmentation quality. The bottom row shows the corresponding histograms from pixels in the
radiologist outline fibroglandular and fatty tissues on each image. Blue and red curves denote the
535 histograms of fibroglandular tissue and fatty tissue, respectively. It clearly shows that the

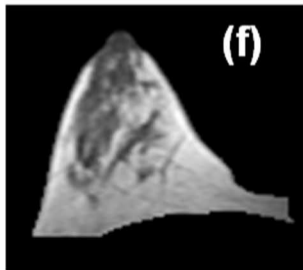
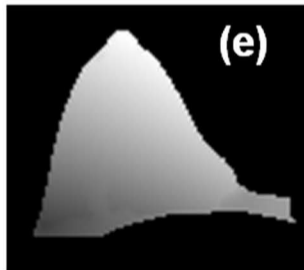
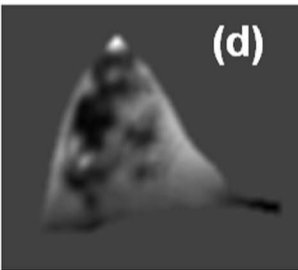
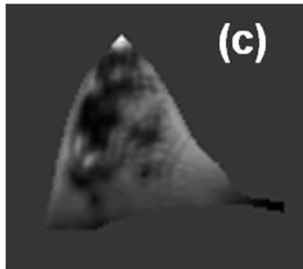
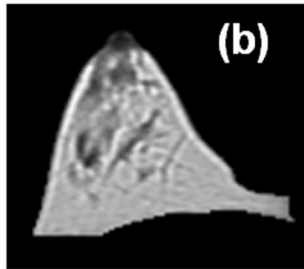
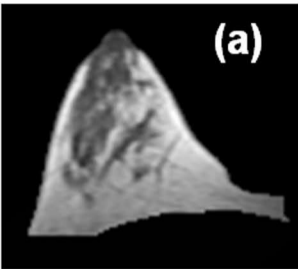
proposed N3+FCM algorithm increases the dynamic range, and widens the separation between the histogram peaks of fatty tissue and fibroglandular tissue.

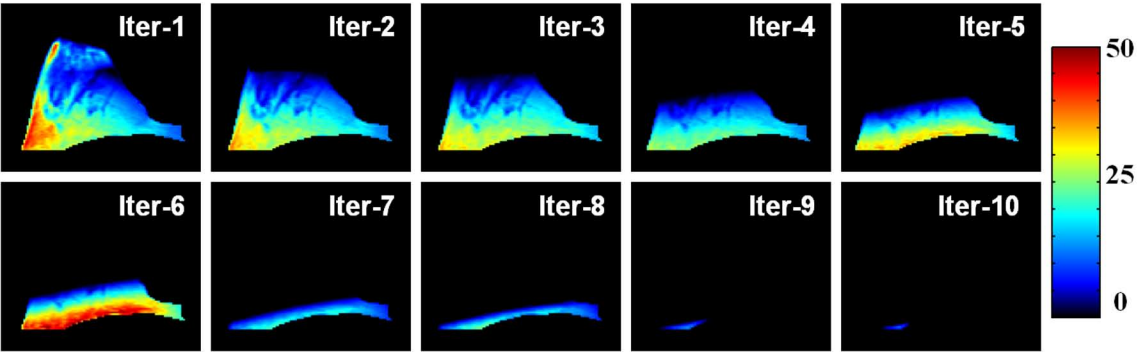
Figure 5. A case example of " $N3+FCM > N3 > FCM$ ". It can be seen that the N3+FCM
540 correction brightens the signal of fatty tissues in the medial posterior breast, and allows the correct classification of pixels in that area as fatty tissues. N3 did not completely correct the bias field, and some tissues in that area are mis-classified as dense tissues. The FCM gives the worst performance. Not only that some fatty tissues in the medial posterior breast are mis-classified as dense tissues, also some dense tissues in the anterior breast close to the nipple are mis-classified
545 as fatty tissues.

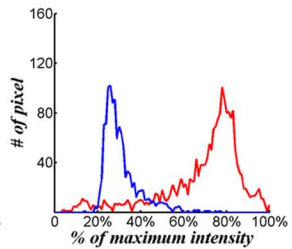
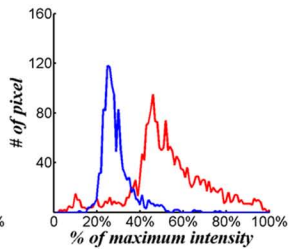
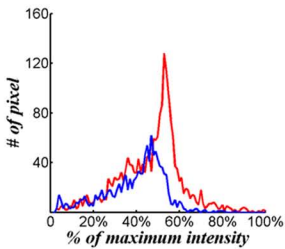
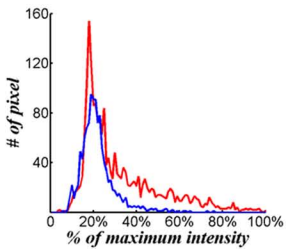
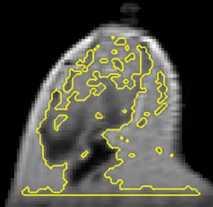
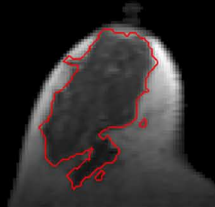
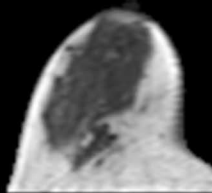
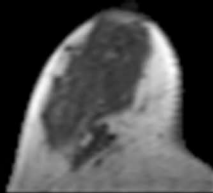
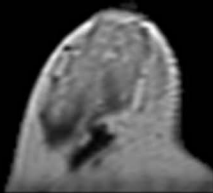
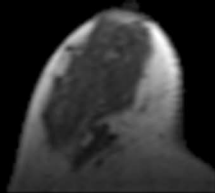
Figure 6. A case example of " $N3+FCM = N3 > FCM$ ". Although the N3+FCM and N3 show slightly different results, both are acceptable, and their performances are rated equal. The same problems indicated in Figure 5 for FCM corrected images (fatty tissues mis-classified as dense
550 tissues and dense tissues mis-classified as fatty tissues) are seen, and that makes the performance of FCM inferior to the other two methods.

Figure 7. A case example of " $N3+FCM = N3 = FCM$ ". The segmentation based all three methods yields similar results, and their performances are rated as equal. Note that this breast is fatter
555 (with a smaller protruding depth into the coil), and there is no visually discernable strong bias field. For this case, the correction is probably not needed, and all three methods perform equally well.

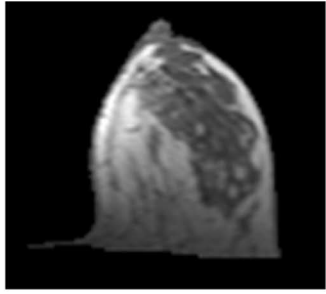




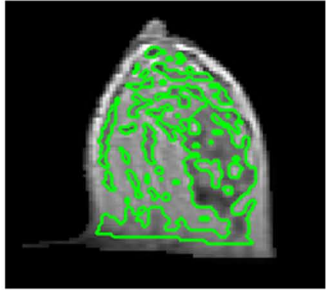
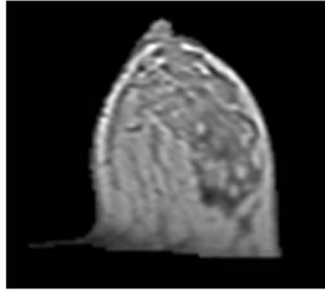


Original**FCM****N3****N3+FCM**

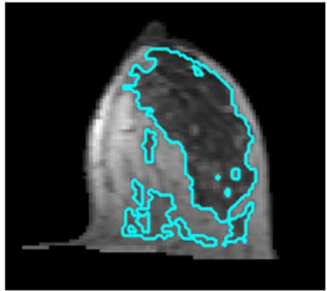
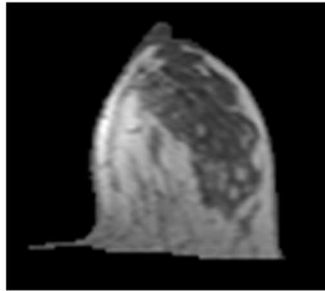
Original



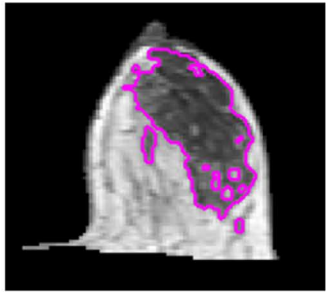
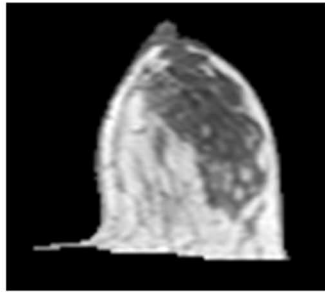
FCM



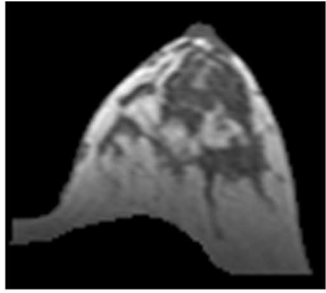
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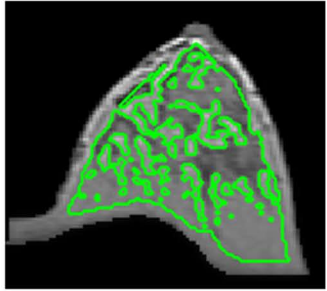
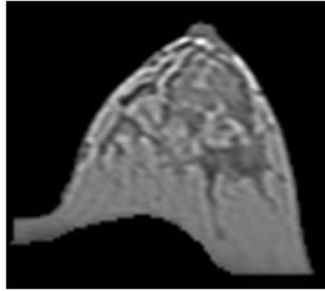
N3+FCM



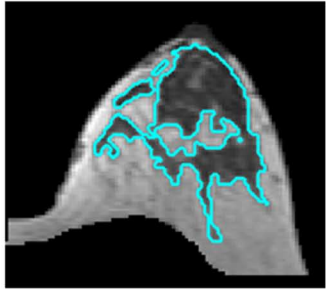
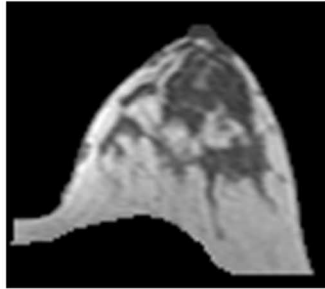
Original



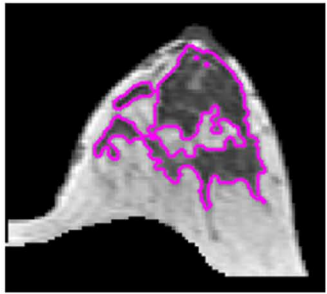
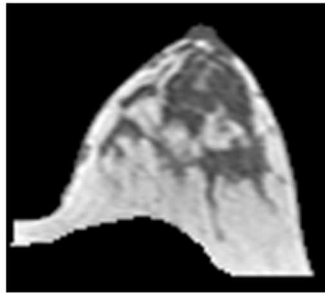
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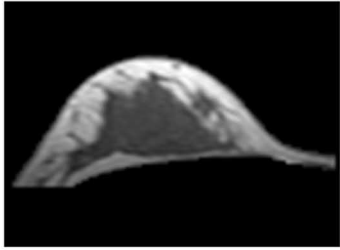
N3



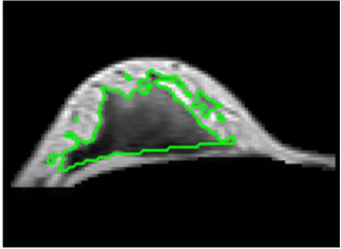
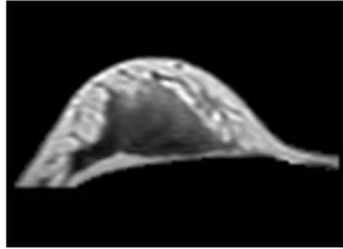
N3+FCM



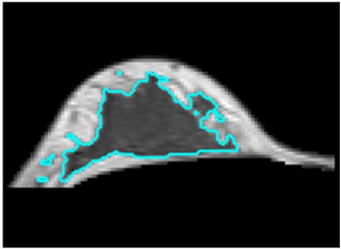
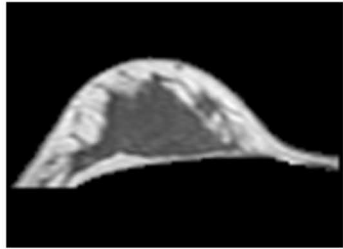
Original



FCM



N3



N3+FCM

